
Subject: Re: Meaning of outer product

Posted by [MKatz843](#) on Sat, 13 Jul 2002 21:30:20 GMT

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> IDL documentation says: "Note - If A and B arguments are vectors, then C =
> MATRIX_MULTIPLY(A, B) is a matrix with $C_{ij} = A_i B_j$. Mathematically, this
> is equivalent to the outer product. . . ." But I'm having difficulty
> reconciling this with my understanding of outer product. . .
>
> $c.x = a.y*b.z - a.z*b.y$
> $c.y = a.z*b.x - a.x*b.z$
> $c.z = a.x*b.y - a.y*b.x$
>

That's the "cross-product" $c = a \times b$ you've written (above).

As you know, the "inner product" of two 3-element vectors is a scalar,
also known as the "dot-product"

$c = a \cdot b = a.x*b.x + a.y*b.y + a.z*b.z$

The inner product is written as a row vector times a column vector.

The "outer product" of two three-element vectors is a 3x3 matrix

C =

($a.x*b.x$ $a.x*b.y$ $a.x*b.z$)

($a.y*b.x$ $a.y*b.y$ $a.y*b.z$)

($a.z*b.x$ $a.z*b.y$ $a.z*b.z$) (I hope this isn't the transpose!)

it's usually written as a column vector times a row vector.

Remember that vector and matrix multiplications aren't necessarily
commutative: $a \text{ times } b \neq b \text{ times } a$, necessarily.

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