
Subject: Re: Transpose(A)*P*A

Posted by [Craig Markwardt](#) on Sat, 11 Oct 2008 19:42:15 GMT

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"mapper4u6@gmail.com" <zjwang2u@gmail.com> writes:

> hello,

>

> I have a question about how to improve the computation speed when deal

> with non-linear equation

> $A \cdot x = I$, P is the weight for each

> row, P is $M \times M$

> $M \times N$ $N \times 1$ $M \times 1$

>

> then I have to build normal matrix which is

> $\text{Transpose}(A) \cdot P \cdot A \cdot x = \text{Transpose}(A) \cdot P \cdot I$

> $N \times N$ $N \times 1$ $N \times 1$

>

> then x can be solved.

I'm going to channel our vice presidential candidate and answer a different question.

It looks like you are trying to solve a least squares problem. It's well documented that the normal equation method suffers from accuracy problems, basically because you are squaring the A matrix, and thus squaring the errors. Have you tried SVD or QR factorization?

Implemented correctly, the execution times should scale as,

Normal equation $\sim N^2 \cdot (M + N/3)$

QR $\sim N^2 \cdot (2M - 2N/3)$

SVD $\sim N^2 \cdot (2M + 11N/3)$

On its face, QR factorization will take longer (not more than double the time though), but it is known to be more stable.

Craig

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