
Subject: Least squares fit of a model to a skeleton consisting out of 3D points.

Posted by [Johan](#) on Mon, 24 Nov 2008 13:33:18 GMT

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I have the following problem to solve and was wondering whether the mpfit routines of Craig Markwardt will do the job?

Do have the following model:

Let $g(X,Y,Z)=1$ be a quadratic function in the coordinate system (O,Z,Y,Z) defined by the long, horizontal and vertical axes (ellipsoid). Write the equation of this quadratic function in matrix notation as follows:

$$g(X,Y,Z) = [X, Y, Z] * [[A1,A4,A5],[A4,A2,A6],[A5,A6,A3]] * [[X],[Y],[Z]] + [X, Y, Z] * [[A7],[A8],[A9]]$$

Need to fit this model to a 3D skeleton of N points by using least squares by calculating the coefficients A_i .

This is achieved by minimizing the total squared error between the exact position of the points (X_i, Y_i, Z_i) on the quadratic surface and their real position in the coordinate system (O, X, Y, Z). The minimizing is performed from the derivative of the equation below with respect to $A_1 \dots A_9$:

$$J(A_1 \dots A_9) = \sum_{i=0}^N (1 - (X_i, Y_i, Z_i))^2$$

This equation yields a linear system of nine equations in which the values of coefficients $A_1 \dots A_9$ are unknown.

Anyone that can help?
Johan Marais
