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Subject: match\_3d.pro

Posted by [Grant K](#) on Thu, 15 Oct 2009 09:38:29 GMT

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Hi,

I was looking for a way to do the nearest neighbour problem in 3D and didn't find anything pre-written that would do it. I've taken J.D. Smith's match\_2d.pro and turned it into match\_3d.pro and have pasted it below for people who might like to use it. I'm not an IDL expert... but it appears to work and the modifications were (thankfully) minimal.

If anyone wants to tidy/fix/streamline it to make an version for more public consumption then go for it.

cheers  
Grant

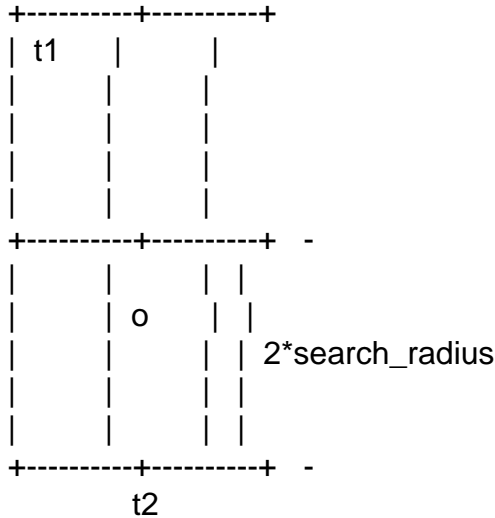
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```
;+
; NAME:
;   MATCH_3D
;
; PURPOSE:
;
;   Perform a match between two sets of 3D coordinates, finding
;   the closest coordinate match (in the Euclidean sense) to the
;   search set, within some search radius. This routine is simply
;   match_2d.pro with an extra dimension added, for those who need
;   to think about where something actually is, rather than where
;   it appears to be on the sky...
;
; CALLING SEQUENCE:
;   match=MATCH_3D
;(x1,y1,z1,x2,y2,z2,search_radius,MATCH_DISTANCE=)
;
; INPUTS:
;
;   x1,y1,z1: The target list to search for matches, of length n1.
;
;   x2,y2,z2: The search list of length n2, to be searched for
;   matches to [x1,y1,z1].
;
;   search_radius: The search radius within which matches will be
;   found. Only if the closest matching coordinate in
; [x2,y2,z2]
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; is within the search radius will it be returned. This is a
; critical variable in tuning the resources required by
; MATCH_3D. It can be a scalar or two element vector (for
; asymmetric radii). See NOTES and WARNING.
;
; KEYWORD PARAMETERS:
;
; MATCH_DISTANCE: On output, the distances between the matches
; and the returned coordinate from the set [x1,y1,z1]
; (<=search_radius), is returned.
;
; OUTPUTS:
;
; match: A 1D vector of length n1 containing the indices of
x2,y2
; and z2 for the closest match to each [x1,y1,z1], within the
; search_radius. If no match was found within the search
; radius, -1 is returned at that location.
;
; EXAMPLE:
;
; n=100000
; x1=randomu(sd,n) & y1=randomu(sd,n) & z1=randomu(sd,n)
; x2=randomu(sd,n) & y2=randomu(sd,n) & z2=randomu(sd,n)
; match=match_3d(x1,y1,z1,x2,y2,z2,.002,MATCH_DISTANCE=md)
;
; SEE ALSO:
;
; HISTOGRAM, HIST_ND
;
; NOTES:
;
; This match program uses HIST_ND to pre-bin the 3D search
; coordinates based on position, within some canonical
; search_radius. See:
;
; http://www.dfanning.com/code\_tips/matchlists.html
;
; for a discussion of its methods. Of principle importance in
; the efficiency and behavior of the match is the SEARCH_RADIUS
; parameter. This is the maximum radial distance within which a
; match point must lie to be returned. Here's a diagram
; illustrating the problem and method in 2D (for 3D simply at an
; extra layer of boxes on top, giving 8 bins). For each target
point,
; four separate bins each of width 2*search_radius are searched
; among the binned search list, depending on its location within
; the bin.

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The point `t2' is the closest to the search point `o', but it is not within the search\_radius, therefore it is not considered. Instead, point `t1' is found (and discarded), despite the fact that `t2' is closer.

Ideally, the search radius should be set to something useful in terms of the match (e.g. positional uncertainty, etc.). However, if the input target coordinates ([x2,y2]) span a large range, it may be necessary to use a larger search radius to avoid an excessively large number of bins. Typically there will be an optimal search radius which is fastest. The tradoff is as follows: the larger the search radius, the smaller the number of bins to search, but the more search points must be considered per target point. The smaller the search radius, the smaller the number of search points per bin, but the greater the number of bins. Something like the median inter-point separation is probably close to optimal.

Since lines of longitude converge towards the poles, a simple trick to obtain roughly the same matching radius in both longitude and latitude is to give an asymmetric search\_radius: [eps/cos(mean(latitude)),eps] for [longitude, latitude]. This works only when the range of latitude is small.

#### WARNING:

Distance is evaluated in a strict Euclidean sense. For

```
; points on a sphere, the distance between two given
; coordinates is *not* the Euclidean distance. As an extreme
; example, consider two points very near the N. pole, but on
; opposite sides (one due E, one due W). For small patches
; away from the poles, this Euclidean assumption is
; approximately valid, and the method works. See NOTES above
; for a tip regarding obtaining a (more) uniform match
; criterion on the sphere. For regions very near the pole, the
; match could be made after suitably projecting all coordinates
; using a map projection which alleviates this behavior.
```

```
..
;
```

#### ``` ; MODIFICATION HISTORY: ```

```
; Thur Oct 2009 (G Kennedy): take match_2d.pro and add z's to
; make match_3d.pro. I take no credit
; for being clever and all responsibility if this routine
doesn't
; work as advertised.
```

```
; Wed Apr 22 17:56:26 2009 (J.D. Smith): Correctly account for
; list ranges and "one bin off" matches.
```

```
; Mon Jul 30 10:56:31 2007, J.D. Smith <jdsmith@as.arizona.edu>
```

```
; Written.
```

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; -
;#####
;#####
```

#### ``` ; LICENSE ```

```
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```

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; Boston, MA 02110-1301, USA.
;
;#####
#####

function
match_3d,x1,y1,z1,x2,y2,z2,search_radius,MATCH_DISTANCE=min_dist
bs = 2*search_radius ;this is the smallest binsize allowed
mx=[max(x2,MIN=mnx2),max(y2,MIN=mny2),max(z2,MIN=mnz2)]
mn=[mnx2,mny2,mnz2]
mn-=1.5*bs & mx+=1.5*bs ;expand the range by (more than) the
bin size
h = hist_nd([1#x2,1#y2,1#z2],bs,REVERSE_INDICES=ri,MIN=mn,MAX=mx )
d = size(h,/DIMENSIONS)

;; Bin location of X1,Y1,Z1 in the X2,Y2,Z2 grid
xoff = 0.> (x1-mn[0])/bs[0] < (d[0]-1.)
yoff = 0.> (y1-mn[1])/(n_elements(bs) gt 1?bs[1]:bs) < (d[1]-1.)
zoff = 0.> (z1-mn[2])/(n_elements(bs) gt 1?bs[2]:bs) < (d[2]-1.)
xbin = floor(xoff) & ybin = floor(yoff) & zbin = floor(zoff)
bin = xbin + d[0]*(ybin + d[1]*zbin) ;The 1D index of the bin
it's in

;; We must search 8 bins worth for closest match, depending on
;; location within bin (i.e. towards any of 8 quadrant directions
;; ul, ur, ll, lr and with back/forward now too...).
xoff = 1-2*((xoff-xbin) lt 0.5) ;add bin left or right
yoff = 1-2*((yoff-ybin) lt 0.5) ;add bin down or up
zoff = 1-2*((zoff-zbin) lt 0.5) ;add bin forward or back

n1=n_elements(x1)
min_pos = make_array(n1,VALUE=-1L)
min_dist = fltarr(n1,/NOZERO)

rad2=search_radius^2

for i=0,1 do begin ;; Loop over 4 bins in the correct quadrant
direction
for j=0,1 do begin
for g=0,1 do begin ;; and one more for z direction

;; One of 8 search bins for all the target points
b = 0L>(bin+i*xoff+j*yoff*d[0]+g*zoff*d[1])<(d[0]*d[1]*d
[2]-1)

;; Dual HISTOGRAM method, loop by count in the search bins
h2 = histogram(h[b],OMIN=om,REVERSE_INDICES=ri2)

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;; Process all bins with the same repeats (>= 1) at a time
for k=long(om eq 0),n_elements(h2)-1 do begin
  if h2[k] eq 0 then continue
  these_bins = ri2[ri2[k]:ri2[k+1]-1] ;bins with k+om
search points

  if k+om eq 1 then begin ; single point
    these_points = ri[ri[b[these_bins]]]
  endif else begin ; range over k+om points, (n x k+om)
    targ=[h2[k],k+om]
    these_points = ri[ri[rebin(b[these_bins],targ,/
SAMPLE)]+ $
                                rebin(lindgen(1,k+om),targ,/
SAMPLE)]
    these_bins = rebin(temporary(these_bins),targ,/
SAMPLE)
  endelse

  ;; Closest distance squared within this quadrant's bin
  dist = (x2[these_points]-x1[these_bins])^2 + $
        (y2[these_points]-y1[these_bins])^2 + $
        (z2[these_points]-z1[these_bins])^2

  if k+om gt 1 then begin ;multiple points in bin: find
closest
    dist = min(dist,DIMENSION=2,p)
    these_points = these_points[p] ;index of closest
point in bin
    these_bins = ri2[ri2[k]:ri2[k+1]-1] ;original bin
list
  endif

  ;; See if a minimum is already set there
  set = where(min_pos[these_bins] ge 0, nset, $
             COMPLEMENT=unset,NCOMPLEMENT=nunset)

  if nset gt 0 then begin
    ;; Only update those where the new point is closer
    closer = where(dist[set] lt min_dist[these_bins
[set]], cnt)
    if cnt gt 0 then begin
      set = set[closer]
      min_pos[these_bins[set]] = these_points[set]
      min_dist[these_bins[set]] = dist[set]
    endif
  endif

  if nunset gt 0 then begin      ;; Nothing set, it's

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```
closest by default
    wh=where(dist[unset] lt rad2,cnt) ;demand it's within
radius
    if cnt gt 0 then begin
        unset=unset[wh]
        min_pos[these_bins[unset]] = these_points[unset]
        min_dist[these_bins[unset]] = dist[unset]
    endif
endif
endfor
endfor
endfor
endfor
if arg_present(min_dist) then min_dist=sqrt(min_dist)
return,min_pos
end
```

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