> I still think that the problem as stated
> is ill-posed.

I agree. If you take away the convex condition (as the OP seems to
ask), then whatever the set of points you can keep reducing the
surrounding area until you get to zero. You'll get some kind of
spidery thing, but it's probably not what he had in mind.

Greg