
Subject: Re: Again an FFT question

Posted by [Kenneth P. Bowman](#) on Wed, 27 Jun 2012 15:53:23 GMT

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In article <614d4d33-39a8-4059-bc5f-f99f08fbc966@googlegroups.com>, Helder <helder@marchetto.de> wrote:

> Dear FFTers,
> I was just wondering about the translation of the FFT so that the what is
> located at (0,0) goes in the middle of the image (N/2,M/2).
> Until now I did this doing simply a shift of the FFT image, that is:
> $\text{FFT_Img} = \text{SHIFT}(\text{FFT}(\text{Img}), N/2, M/2)$
> Now I have seen that some people use a FFT "trick" to shift the image. They
> switch every second pixel of an image to its negative value. This is
> justified by the translation properties of the DFTs and results in a
> translation of half the image size (for those seeking to understand the math,
> try to multiply the function (image) by $\exp(i \cdot 2 \cdot \pi \cdot (u_0 \cdot x / N))$ and after
> integration you will get a translation of the Fourier image (signal for 1D)
> of $F(u-u_0)$.

>
> The result is that the two are not exactly the same. Very similar, but not
> the same.
> I have tried varying the size of the image or switching even instead of odd
> numbers index numbers , but could not get any improvement (with odd image
> sizes, the difference is even higher).
>
> Does anybody have a reason to use one way ($\text{shift}(\text{fft}(\text{Img}...))$) rather than
> the other (switch pixels with index $((x+y) \bmod 2 \text{ EQ } 1)$)?
>
> I'm more confident using SHIFT, but I would just like to understand why the
> other method gives different values.
>
> Thanks,
> Helder

If you do an FFT of an 8-point array, the output frequencies are stored in this order

$f = [0, 1, 2, 3, 4, -3, -2, -1]$

The IDL FFT always does a complex FFT. If the input data are real, then the real part of $f=0$ is the mean, the imaginary part is 0 to within roundoff error.

The positive and negative frequencies are complex conjugates of each other - again within roundoff error.

I think the differences that you are seeing are due to round-off error. Check the magnitudes of the differences.

Ken Bowman
