
Subject: Re: regression with 95% confidence interval
Posted by [ftian2012](#) on Mon, 06 Mar 2017 10:04:20 GMT
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On Monday, July 22, 2013 at 5:57:47 PM UTC+2, KenBowman wrote:

> On 2013-07-22 15:11:51 +0000, Fabien said:

>

>> On 07/22/2013 03:35 PM, Kenneth Bowman wrote:

>> I e-mailed you a routine that will compute confidence limits on the

>>> slope and intercept.

>>

>> I am interested in your method too ;-). Could you mail it to me too?

>

> It is a short routine, so I have pasted it below.

>

> The function computes a linear regression and confidence limits on the

> slope and intercept following the examples in Tamhane and Dunlop, which

> robustness of the confidence limits depends on whether the underlying

> statistics of the process in question satisfy the assumptions that are

> is assumed to be known with no error, and the error in the predictand

> for more details.

>

> Cheers, Ken

>

>

> FUNCTION REGRESSION_STATISTICS_KPB, x, y, \$

> CI = ci, \$

> DOUBLE = double, \$

> VERBOSE = verbose

>

>

> ;+

> ; Name:

> ; REGRESSION_STATISTICS_KPB

> ; Purpose:

> ; This program computes the regression coefficients a and b and
> their confidence limits

> ; for simple bivariate linear regression

> ;

> ;

> ; $y = a + b \cdot x + \text{eps}$

> ;

> ; The calculations follow the exposition in Chap. 10 of Tamhane and
> Dunlop (2000).

> ; Calling sequence:

> ; stats = REGRESSION_STATISTICS_KPB(x, y[, ci])

```

> ; Inputs:
> ;   x      : Values of the independent variables.
> ;   y      : Values of the independent variables.
> ; Output:
> ;   stats  : Data structure containing various statistics and
> confidence limits.
> ; Keywords:
> ;   CI      : Optional confidence limit (%). If not set, a default
> value of 95% is used.
> ;   VERBOSE : If set, print the statistics and confidence intervals.
> ; Author and history:
> ;   Kenneth P. Bowman. 2007-11-01.
> ;-
>
> IF (N_PARAMS() NE 2) THEN MESSAGE, 'Incorrect number of arguments.'
> ;Check number of arguments
>
> IF (N_ELEMENTS(ci) EQ 0) THEN ci = 95.0D0
> ;Default confidence limit to calculate
>
> n = N_ELEMENTS(x)
> ;Number of data points
> IF (N_ELEMENTS(y) NE n) THEN $
> ;Check array sizes
> MESSAGE, 'The number of x and y values must be equal.'
>
> b = (REGRESS(x, y, CONST = a, YFIT = yfit, FTEST = f_stat, $
> ;Compute regression and extract value of b
> CORRELATION = r, CHISQ = chisq, DOUBLE = double))[0]
>
> s = SQRT(TOTAL((yfit - y)^2)/(n-2))
> ;Standard deviation of the residuals
> x_mean = MEAN(x)
> ;Mean of the x values
> y_mean = MEAN(y)
> ;Mean of the y values
> S_xx = TOTAL((x - x_mean)^2)
> ;Sum of the squared deviations of x from the mean
> S_yy = TOTAL((y - y_mean)^2)
> ;Sum of the squared deviations of y from the mean
> S_xy = TOTAL((x - x_mean)*(y - y_mean))
> ;Sum of the products of the deviations of x and y from their
> means
> SE_a = s*SQRT(TOTAL(x^2)/(n*S_xx))
> ;Standard error of a
> SE_b = s/SQRT(S_xx)
> ;Standard error of b
> alpha = (1.0D0 - 0.01D0*ci)/2.0D0

```

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> ;Level for t-test
> t_stat = T_CVF(alpha, n-2)
> ;Compute t-statistic
>
> IF KEYWORD_SET(verbose) THEN BEGIN
>   PRINT, 'Intercept (a)      : ', a
>   PRINT, 'Slope (b)         : ', b
>   PRINT, 'Correlation coefficient r : ', r
>   PRINT, 'r^2                : ', r^2
>   PRINT, 'F-statistic        : ', f_stat
>   PRINT, 'Chi-square statistic : ', chisq
>   PRINT, 'n                  : ', n
>   PRINT, 'Mean of x          : ', x_mean
>   PRINT, 'Mean of y          : ', y_mean
>   PRINT, 'S.D. of residuals  : ', s
>   PRINT, 'S_xx               : ', S_xx
>   PRINT, 'S_yy               : ', S_yy
>   PRINT, 'S_xy               : ', S_xy
>   PRINT, 'S.E. of a          : ', SE_a
>   PRINT, 'S.E. of b          : ', SE_b
>   PRINT, 'Confidence limit    : ', ci, '%'
>   PRINT, 'Level for t-test    : ', alpha
>   PRINT, 't-statistic         : ', t_stat
>   PRINT, 'Confidence interval for a : ', a, '+/-',
>   STRTRIM(t_stat*SE_a, 2), ' [', a - t_stat*SE_a, ', ', a + t_stat*SE_a,
>   ']'
>   PRINT, 'Confidence interval for b : ', b, '+/-',
>   STRTRIM(t_stat*SE_b, 2), ' [', b - t_stat*SE_b, ', ', b + t_stat*SE_b,
>   ']'
> ENDIF
>
> RETURN, {a      : a,      $
> ;Y-intercept
>   b      : b,      $
> ;Slope
>   r      : r,      $
> ;Correlation coefficient r
>   yfit    : yfit,    $
> ;Fitted values at x
>   f_stat   : f_stat,  $
> ;F-statistic
>   chisq    : chisq,   $
> ;Chi-squared statistic
>   n        : n,      $
> ;Number of points
>   x_mean   : x_mean,  $
> ;Mean of the x values
>   y_mean   : y_mean,  $

```

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> ;Mean of the y values
>      s      : s,      $
> ;Standard deviation of the residuals
>      S_xx    : S_xx,    $
> ;Sum of the squared deviations of x from its mean
>      S_yy    : S_yy,    $
> ;Sum of the squared deviations of y from its mean
>      S_xy    : S_xy,    $
> ;Sum of the products of the deviations of x and y from their means
>      SE_a    : SE_a,    $
> ;Standard error of a
>      SE_b    : SE_b,    $
> ;Standard error of b
>      ci      : ci,      $
> ;Requested confidence interval (%)
>      alpha   : alpha,   $
> ;Level for t-test
>      t_stat  : t_stat,  $
> ;t-statistic value
>      ci_a    : t_stat*SE_a, $
> ;Confidence interval for a is (a +/- ci_a)
>      ci_b    : t_stat*SE_b }
> ;Confidence interval for b is (b +/- ci_b)
>
> END

```

Thank you very much KenBowman for sharing your excellent code!
