
Subject: mesh_volume and tetra_volume

Posted by [robertschaefer](#) on Mon, 09 Aug 2004 09:24:42 GMT

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Hello, I want to get the volume out of a 3d object.
First i tried with mesh_volume, but the returned values weren't similar to my calculated. I checked with mesh_issolid: return value:1, so it ios solid and should return the volume.
When i check with tetra_volume the volume is similar to my calculated volume.

Now my question: what is the difference between mesh_volume and tetra_volume?

Robert

Subject: Re: mesh_volume and tetra_volume

Posted by [Karl Schultz](#) on Tue, 10 Aug 2004 16:19:12 GMT

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"Robert Schaefer" <robertschaefer@gmx.de> wrote in message news:bffaee64.0408100002.6f8cf5ef@posting.google.com...

> "Karl Schultz" <kschultz_no_spam@rsinc.com> wrote in message news:<10hf9gscqmtjdj41@corp.supernews.com>...

>> "Robert Schaefer" <robertschaefer@gmx.de> wrote in message >> news:bffaee64.0408090124.5906ed23@posting.google.com...

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>>> similar to my calculated. I checked with mesh_issolid: return value:1,

>>> so it ios solid and should return the volume.

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>>> volume.

>>>

>>> Now my question: what is the difference between mesh_volume and

>>> tetra_volume?

>>

>> MESH_VOLUME works by summing:

>>

>> (a dot (b cross c)) / 6

>> for every triangle in the mesh where a, b, and c are the verts of each

>> triangle in the mesh. This effectively calculates the signed volume of

a

>> tetrahedron formed by the origin and the 3 triangle verts for each

triangle

>> and then adds them up.

>>

>> TETRA_VOLUME just adds up the volume of all the tets in the mesh using

the

>> same idea as above.

>>

>> How big a difference are you seeing? Is there anything strange about your

>> mesh, like being self-intersecting? How did you generate both the polygonal

>> mesh and the tetrahedral mesh?

>>

>> Karl

>

> My testobjekt is generated by dilatation of one point. I can not see

> any strange about the mesh.

> With computemesh i generate the triangles, like D.fanning in his

> example (http://www.dfanning.com/graphics_tips/mesh.html). I signed

> the calculated values between tetra_volume and mesh_volume are very

> different:

>

> accord sphere formula : $4./3.*\pi*16.^3 = 17157.3$

> total (vol) : 17611.0

> volume with tetra_volume: 16308.0

> mesh_volume : 11988.0

>

> Any idea?

>

> Robert

Not really. I think I'd have to see your code to understand better what is going on.

Here is an example that might help.

It makes a volume where each sample value is the distance from the volume center.

I use that to create an isosurface where the isovalue is some arbitrary radius value.

I print out the ideal volume of the sphere and then the volume of the isosurface according to MESH_VOLUME.

I don't know how you are getting your tetrahedral mesh, but I use INTERVAL_VOLUME and then use TETRA_VOLUME to compute the volume that way. I also extract the surface of the tet mesh and compute the volume enclosed by that with MESH_VOLUME.

The results are printed below. Note that all of the values except the ideal volume are very close. The reason why the ideal volume is a bit different

is because the volume is performing discrete sampling, and so there is sampling error . The volumes of the various meshes will approach the ideal volume as you increase sampling.

I hope this helps you solve your problem.

Karl

```
pro t
  n = 40
  mid = n / 2
  radius = n / 3.5
  vol = BYTARR(n,n,n)
  for i=0, n-1 do begin
    for j=0, n-1 do begin
      for k=0, n-1 do begin
        vol[i,j,k] = SQRT( (i-mid)^2 + (j-mid)^2 + (k-mid)^2 ) + 0.5
      endfor
    endfor
  endfor

  ISOSURFACE, vol, radius, v, c

  print, "Ideal volume", 4./3.*!pi*radius^3
  print, MESH_ISSOLID(c)
  print, "Isosurface volume", MESH_VOLUME(v, c)

  INTERVAL_VOLUME, vol, 0, radius, tet_verts, tet_conn
  print, "Tetrahedral volume", TETRA_VOLUME(tet_verts, tet_conn)
  surf_conn = TETRA_SURFACE(tet_verts, tet_conn)
  print, MESH_ISSOLID(surf_conn)
  print, "Tetrahedral volume by surface", MESH_VOLUME(tet_verts,
surf_conn)
end
```

```
IDL> t
Ideal volume 6252.66
1
Isosurface volume 6321.85
Tetrahedral volume 6321.87
1
Tetrahedral volume by surface 6321.85
```

Subject: Re: mesh_volume and tetra_volume

Posted by [robertschaefer](#) on Mon, 16 Aug 2004 15:34:00 GMT

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Hello,

I tried to binarize your calculation like this :

ISOSURFACE, vol1 lt radius, 1, v, c

-> i tried with : print,mesh_issolid(tc)

% MESH_ISSOLID: Invalid polygon connectivity.

after that i took the mesh_issolid(tetra_surface(tv,tc))
function and returned a solid connectivity.

I dont understand why i can not check mesh_issolid
directly after calculating the verts and conns with isosurface
and have to take Interval_volume.

Second i do not understand the treshold from isosurface,
which values i have to choose.

thanks for any ideas.

Robert

Subject: Re: mesh_volume and tetra_volume

Posted by [Karl Schultz](#) on Mon, 16 Aug 2004 16:24:51 GMT

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"Robert Schaefer" <robertschaefer@gmx.de> wrote in message
news:bffaee64.0408160734.11b17727@posting.google.com...

> Hello,

> I tried to binarize your calculation like this :

> ISOSURFACE, vol1 lt radius, 1, v, c

> -> i tried with : print,mesh_issolid(tc)

> % MESH_ISSOLID: Invalid polygon connectivity.

Looks like you are passing a tet mesh conn list to mesh_issolid. Tet meshes
are always solid. Plus, the tet mesh conn lists are a different format than
the polygon conn lists.

You should be using the variable c, not tc.

>

> after that i took the mesh_issolid(tetra_surface(tv,tc))

> function and returned a solid connectivity.

> I dont understand why i can not check mesh_issolid

> directly after calculating the verts and conns with isosurface

> and have to take Interval_volume.

You can if you do:

ISOSURFACE, vol, isovalue, v, c
print, MESH_ISSOLID(c)

>
> Second i do not understand the treshold from isosurface,
> which values i have to choose.

Do you mean isovalue?

It depends on the range of values in the volume and what values you want the surface to represent.

>
> thanks for any ideas.
>
> Robert

Subject: Re: mesh_volume and tetra_volume
Posted by [robertschaefer](#) on Wed, 18 Aug 2004 11:41:32 GMT
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Hello,
thanks for your help so far but there are some questions ;-)
I try to understand how Interval_volume and Isosurface works.
I have Problems to calculate the volume because in my real objekts
i do not know the radius. In Your code and my testobject we use
approximately a sphere. When i use other values (for example :
INTERVAL_VOLUME, vol, 0.1, 0.6, tet_verts, tet_conn)the results
are different, thats clear. But how do i know which values are
the right for my object to calculate the right volume?
I watched at the idl-example "Interval_volume" and explored the changes
in xobjectview when maybe the first value set 0-> i get a box. i think
thats clear, because i watch at a different range. What do you think
can i do?
The same problems occure by testing with isosurface. I don't understand
when mesh is solid and how to choose the value when there is no given
radius or not a spherical objekt.
(my examples: -ISOSURFACE,vol,1,v,c
->mesh_issolid = 1,3333
->mesh_volume(v,c)=6,6666
-ISOSURFACE,vol,2,v,c
->mesh_issolid = 0
-ISOSURFACE, vol, 1.9, v, c
->mesh_volume(v,c)=27,43
-INTERVAL_VOLUME, vol, 0.1, 0.5, tet_verts, tet_conn
->tetra_volume = 23,2374)

you described : "It depends on the range of values in the volume and what values you want the surface to represent." i get values by verts and conns (coordinates and conn-length). that might be enough to calculate a volume...

There must be any way ;-) ?!?

Robert

Subject: Re: mesh_volume and tetra_volume
Posted by [Karl Schultz](#) on Wed, 18 Aug 2004 17:34:38 GMT
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In your specific case, if you have a volume that describes an object in such a way that the volume is filled with 0's where the object does not exist, and then 1's where it does exist, then there is no "radius". You should be able to just use the isovalue of 1. This will place the isosurface on the outer surface of your "object", which is what I think you want.

Example:

```
IDL> vol = bytarr(30,30,30)
IDL> vol[13:15, 13:15, 13:15] = 1
IDL> isosurface, vol, 1, v, c
IDL> xobjview, OBJ_NEW('IDLgrPolygon', v, polygons=c)
IDL> print, MESH_VOLUME(v,c)
0.000000
IDL> r = MESH_VALIDATE(v,c,/combine)
IDL> print, MESH_VOLUME(v,c)
8.00001
```

I set 3x3x3 samples near the middle of the volume to 1 to represent the extents of my little cube. The extents enclose a volume of 2x2x2, which is 8.

Here's some more info that I thought I'd pass along.

People generate isosurfaces to look at volume data collected from some sort of device. And they know precisely what the values in volume represent. For example, if you have a 3D scan of a human head, you might know that skin values are represented in the range 10-20 (out of a range from 0-255). If you construct an isosurface from this volume using an isovalue of 18 or something, you'll get a pretty good surface that approximates the skin. (I'm making up these values)

```
IDL> head = READ_BINARY(FILEPATH('head.dat', SUBDIRECTORY=['examples',
```

```
'data']], DATA_DIMS=[80,100,57])  
IDL> isosurface, head, 18, v, c  
IDL> xobjview, OBJ_NEW('IDLgrPolygon', v, polygons=c)
```

Maybe it is easier to look at a simpler example:

```
IDL> vol = BYTARR(3,3,3)  
IDL> vol[1:2,*,*]=1  
IDL> isosurface, vol, 0.5, v, c  
IDL> print, v  
0.500000 0.000000 0.500000  
0.500000 0.500000 0.000000  
0.500000 0.000000 0.000000  
0.500000 0.000000 1.000000  
0.500000 0.500000 1.000000  
0.500000 1.000000 0.500000  
0.500000 1.000000 0.000000  
0.500000 1.000000 1.000000  
0.500000 1.500000 0.000000  
0.500000 2.000000 0.500000  
0.500000 1.500000 1.000000  
0.500000 2.000000 1.000000  
0.500000 2.000000 0.000000  
0.500000 0.000000 1.500000  
0.500000 1.000000 1.500000  
0.500000 0.500000 2.000000  
0.500000 1.000000 2.000000  
0.500000 0.000000 2.000000  
0.500000 1.500000 2.000000  
0.500000 2.000000 1.500000  
0.500000 2.000000 2.000000  
IDL> xobjview, OBJ_NEW('IDLgrPolygon', v, polygons=c)
```

The volume is a small cube where 1/3 of the volume is a "slab" with sample values of 0, and 2/3 a thicker slab with sample values of 1. If you want to find the isosurface with isovalue of 0.5, it would split the thinner slab in two, because that one-voxel-wide slab would have samples of 0 on one side and samples of 1 on the other. The isosurface, with a value of 0.5, must pass through the volume so that all points on the isosurface are the same distance from samples of value 0 and samples of value 1. That is the basic nature of an isosurface.

So, the isosurface is a simple plane that is located at $x = 0.5$. See the vertex list above. You can view it with xobjview. You'll need to rotate it because it is edge-on and set the drag quality to low if you want to see the mesh.

It just happens that the sample values in this case coincide with the volume

coords. I could also do:

```
IDL> vol = bytarr(3,3,3)
IDL> vol[0,*,*] = 200
IDL> vol[1:2,*,*]=201
IDL> isosurface, vol, 200.5, v, c
IDL> print,v
```

and get the exact same vertices as above. The point is that the isovalue is exactly the average of the samples at vol[0,*,*] and vol[1,*,*] and so the isosurface must pass through [0.5, *, *].

Now let's try an interval volume.

```
IDL> vol = BYTARR(3,3,3)
IDL> vol[1,*,*]=1
IDL> vol[2,*,*]=2
IDL> interval_volume, vol, 0.5, 1.5, v, c
IDL> c2 = tetra_surface(v,c)
IDL> xobjview, OBJ_NEW('IDLgrPolygon', v, polygons=c2)
```

Same idea here except that my volume is three slabs with values 0, 1, and 2. I constructed an interval volume that bisects each slab along the X direction. So I end up with a box that extends from 0.5 to 1.5 in X and covers the entire volume in Y and Z.

I hate to repeat myself, but you really have to know your data and know what you want to get out of it if you intend to make isosurface and interval volume work for you. Outside of some test volumes we've discussed, I'm not clear on what you are trying to do.

If we go back to the sphere:

```
n = 40
mid = 20
radius = 10
vol = BYTARR(n,n,n)
for i=0, n-1 do begin
  for j=0, n-1 do begin
    for k=0, n-1 do begin
      vol[i,j,k] = SQRT( (i-mid)^2 + (j-mid)^2 + (k-mid)^2 ) + 0.5
    endfor
  endfor
endfor
```

```
ISOSURFACE, vol, radius, v, c
```

```
print, "Ideal volume", 4./3.*pi*radius^3
```



```
print, 'Isosurface is ', MESH_ISSOLID(c) ? 'solid' : 'not solid'  
print, "Isosurface volume", MESH_VOLUME(v, c)
```

```
Ideal volume 4188.79  
Isosurface is not solid  
Isosurface volume 0.000000
```

So, my volume is 40x40x40 and I fill in the sample values so that each sample value is the distance from the "center" that I have chosen at 20,20,20. So the volume is now a "field" of samples where the sample value is zero at 20,20,20 and the sample values increase as they are farther from the center. The maximum value is about 35 ($20 * \sqrt{3}$) and occurs in the corners of the volume.

Now I can pick any isovalue I want. If I pick something bigger than 35, there are no samples in the volume larger than 35, so ISOSURFACE will not generate a surface. For example, if I pick 45, the isovalue of 45 does not fall between any two samples in the volume. If I pick something between 20 and 35, I get a clipped sphere.

But if I pick something like 10, I should get a solid sphere. But I don't, as in the above example. Here's why.

Sometimes ISOSURFACE generates coincident vertices - multiple vertices that are located at the same point in space. There is code in ISOSURFACE to prevent this, so this might be a bug (I'll look at it for the next release). The coincident vertices don't have too much effect on the visual appearance of the mesh, but they do confuse analysis functions like MESH_VOLUME.

But the good news is that it is easily fixed by adding:

```
result = MESH_VALIDATE(v, c, /COMBINE_VERTICES)
```

right after the call to ISOSURFACE. Now IDL reports the mesh as being solid and reports a valid volume. I don't know if this was causing your confusion or not.

For more fun, we can do an interval volume with the same volume data:

```
INTERVAL_VOLUME, vol, 5, 10, tet_verts, tet_conn  
result = TETRA_CLIP([1,0,0,-20], tet_verts, tet_conn, verts_out,  
conn_out)  
surf_conn = TETRA_SURFACE(verts_out, conn_out)  
XOBJVIEW, OBJ_NEW('IDLgrPolygon', verts_out, POLYGONS=surf_conn,  
COLOR=[0,0,255])
```

This makes a sphere with a hollow center. I cut it in half with the TETRA_CLIP function and then make a surface that I can look at.

The following makes hyperbolic surfaces:

```
n = 40.0
vol = FLTARR(n,n,n)
a = (3.14159)^2 / 16.0
for i=0, n-1 do begin
  for j=0, n-1 do begin
    for k=0, n-1 do begin
      vol[i,j,k] = a * (i/n-0.5)^2 + a * (j/n-0.5)^2 +
(a-1)*(k/n-0.5)^2
    endfor
  endfor
endfor
```

```
ISOSURFACE, vol, 0, v, c
```

```
XOBJVIEW, OBJ_NEW('IDLgrPolygon', v, POLYGONS=c, COLOR=[0,0,255])
```

And finally, note that back in the sphere case, you can get a much nicer sphere if you don't round off the distances to integers. You can do this by simply changing the volume data type to float:

```
n = 40
mid = n / 2
radius = 10
vol = FLTARR(n,n,n)
for i=0, n-1 do begin
  for j=0, n-1 do begin
    for k=0, n-1 do begin
      vol[i,j,k] = SQRT( (i-mid)^2 + (j-mid)^2 + (k-mid)^2 ) + 0.5
    endfor
  endfor
endfor
```

```
ISOSURFACE, vol, radius, v, c
xobjview, obj_new('idlgrpolygon', v, polygons=c)
```

I hope that this helps you understand all this in general.

Karl

"Robert Schaefer" <robertschaefer@gmx.de> wrote in message
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