Subject: How to speed up KRIG2D by 30x Posted by Mike[5] on Tue, 08 Oct 2013 14:51:57 GMT

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While trying to figure out what the KRIG2D routine was doing, I discovered it can be speed up by one order of magnitude or more, for large numbers of output points.

One only needs to change a single line of code.

I post this here hoping someone at EXELIS will see it and include in the next IDL distribution...

In practice the last few lines of the current KRIG2D routine (as of IDL 8.2.3) should be changed from this

```
for j=0,ny-1 do begin
                           ;Each output point
 v0 = bounds[1] + qs[1] * i
 for i=0,nx-1 do begin
  x0 = bounds[0] + qs[0] * i
  d[0] = reform(sqrt((x-x0)^2 + (y-y0)^2),n); distance
  d = call_function(fname, d, t)
                                  :Get rhs
  d[n] = 1.0
                            :lagrange constr
  d=LUSOL( a, indx, d)
                                 ;Solve using LUDC results.
  r[i,i] = total(d * z)
 endfor
endfor
```

into the following mathematically equivalent form, with LUSOL outside the double FOR loop and a change in the order of the array operations. This works because array multiplication is commutative.

```
az = LUSOL(a, indx, [z,0.0])
                                   ;Solve using LUDC results.
for j=0,ny-1 do begin
                                ;Each output point
 v0 = bounds[1] + gs[1] * j
 for i=0,nx-1 do begin
  x0 = bounds[0] + qs[0] * i
  d[0] = reform(sqrt((x-x0)^2 + (y-y0)^2),n); distance
  d = call function(fname, d, t)
                                :Get rhs
  d[n] = 1.0
                            ;lagrange constr
  r[i,j] = total(d * az)
 endfor
endfor
```

In the following example, with a large number of output points, my modified routine KRIG2D_MODIFIED is 30x faster than IDL's KRIG2D and also 7x faster than the native code

GRIDDATA. This suggests that GRIDDATA is making the same mistake as KRIG2D of including the back substitution inside the final for loop.

```
: Create a dataset of N points.
n = 500;# of scattered points
seed = -121147L :For consistency
x = RANDOMU(seed, n)
y = RANDOMU(seed, n)
: Create a dependent variable in the form a function of (x,y)
z = 3 * EXP(-((9*x-2)^2 + (7-9*y)^2)/4) + $
  3 * EXP(-((9*x+1)^2)/49 - (1-0.9*y)) + $
  2 * EXP(-((9*x-7)^2 + (6-9*y)^2)/4) - $
  EXP(-(9*x-4)^2 - (2-9*y)^2)
s = [0.5,0]
tic
z2 = krig2d_modified(z, x, y, EXPONENTIAL=s, NX=200, NY=200)
toc
tic
z2 = GRIDDATA(x, y, z, /KRIGING, DIMENSION=[200,200], VARIOGRAM=[2,s])
toc
tic
z2 = krig2d(z, x, y, EXPONENTIAL=s, NX=200, NY=200)
toc
```

Subject: Re: How to speed up KRIG2D by 30x Posted by timothyja123 on Wed, 09 Oct 2013 02:59:54 GMT View Forum Message <> Reply to Message

You should probably put in a support request to Exelis rather than just hoping they see this post. That way it will be in their system and is less likely to get lost and forgotten about.

Subject: Re: How to speed up KRIG2D by 30x Posted by chris_torrence@NOSPAM on Wed, 09 Oct 2013 17:32:53 GMT View Forum Message <> Reply to Message

Hi Mike,

This is fantastic. I'm working on adding in your change. However, I just found a different problem.

If you look at the "Krig_Sphere" function within krig2d.pro, the code doesn't match the docs. The documentation states that for spherical covariance:

```
C(d) = C1 - 1.5 C1 (d/A) + 0.5 C1 (d/A)^3 \text{ if } d < A
= C0 + C1 \text{ if } d = 0
= 0 \text{ if } d > A
```

Note that I threw in a factor of C1 on the first line (the docs are wrong).

```
Here is the code:

FUNCTION Krig_sphere, d, t

r = d/t[0]

v = t[1] + t[2] * (r * (1.5 - 0.5 * r *r) > 0)

z = where(d eq 0, count)

if count ne 0 then v[z] = 0

return, (t[1] + t[2]) - v

end
```

We are not clipping to 0 for d > A. In fact, for d > A, the function actually starts to go back up and levels off at the constant C1. You can see this with the following plot:

```
p = plot(krig\_sphere(findgen(40), [10, 0.5, 1]))
```

```
I think the code should be something more like:
```

```
FUNCTION Krig_sphere, d, t
r = d/t[0]
v = t[2] * (1 - r * (1.5 - 0.5*r*r))
v[WHERE(d eq 0, /NULL)] = t[1] + t[2]
v[WHERE(d gt t[0], /NULL)] = 0
return, v
end
```

Thoughts?

-Chris IDL Product Lead ExelisVIS

Subject: Re: How to speed up KRIG2D by 30x Posted by Mike[5] on Thu, 10 Oct 2013 11:44:05 GMT View Forum Message <> Reply to Message

Hi Chris,

Thank you for your prompt response.

You are right, I did notice the covariances were not right. I rewrote them as variograms instead, like below:

```
FUNCTION Krig_sphere, rad, c ;Return Spherical variogram Fcn
  r = rad/c[0] < 1.0
  return, c[1] + c[2] * (r*(1.5 - 0.5*r^2))
end
FUNCTION Krig_expon, rad, c
                                  ;Return Exponential variogram Fcn
  return, c[1] + c[2] * (1.0 - exp(-3.0*rad/c[0]))
end
Another small change I made was to use the two lines below instead of the double loop to fill the
array coefficients
a[0,0] = distance_measure( transpose([[x],[y]]), /MATRIX )
a = call_function(fname, a, t); Get coefficient matrix
On Wednesday, October 9, 2013 6:32:53 PM UTC+1, Chris Torrence wrote:
> Hi Mike.
>
>
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>
>
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>
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>
     = 0
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>
>
>
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>
>
   v = t[1] + t[2] * (r * (1.5 - 0.5 * r *r) > 0)
>
   z = where(d eq 0, count)
```

```
>
   if count ne 0 then v[z] = 0
>
   return, (t[1] + t[2]) - v
>
>
  end
>
>
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>
   v[WHERE(d eq 0, /NULL)] = t[1] + t[2]
>
   v[WHERE(d gt t[0], /NULL)] = 0
>
   return, v
>
  end
>
>
>
  Thoughts?
>
>
  -Chris
> IDL Product Lead
> ExelisVIS
```

Subject: Re: How to speed up KRIG2D by 30x Posted by chris_torrence@NOSPAM on Thu, 10 Oct 2013 16:28:27 GMT

```
On Thursday, October 10, 2013 5:44:05 AM UTC-6, Mike wrote:
> Hi Chris,
>
>
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>
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  FUNCTION Krig_sphere, rad, c
                                     ;Return Spherical variogram Fcn
>
    r = rad/c[0] < 1.0
>
>
     return, c[1] + c[2] * (r*(1.5 - 0.5*r^2))
>
>
> end
>
 FUNCTION Krig_expon, rad, c
                                     ;Return Exponential variogram Fcn
>
     return, c[1] + c[2] * (1.0 - exp(-3.0*rad/c[0]))
>
>
  end
>
>
>
> Another small change I made was to use the two lines below instead of the double loop to fill
the array coefficients
>
>
> a[0,0] = distance_measure( transpose([[x],[y]]), /MATRIX )
> a = call_function(fname, a, t) ; Get coefficient matrix
>
>
Hey Mike,
So when you are using the variograms, what does the rest of the code look like? I just want to
make sure that we get the same answer.
```

-Chris

Subject: Re: How to speed up KRIG2D by 30x Posted by chris_torrence@NOSPAM on Thu, 10 Oct 2013 17:48:56 GMT View Forum Message <> Reply to Message

Okay, here is the new code, minus the comments. I added 3 new keywords: DOUBLE, XOUT, YOUT. DOUBLE forces double precision. XOUT, YOUT are output keywords that contain the final X/Y locations. I also vectorized the final loop, for even more speed.

I also changed the C code of GRIDDATA to move the LUSOL out of the loop.

Now, with Mike's changes and the vectorization, I'm getting the following results using Mike's test code at the top with 500 input points and 400 output points:

Old KRIG2D: 30 seconds New KRIG2D: 0.51 seconds New GRIDDATA: 1.3 seconds

It's funny that the KRIG2D is faster than GRIDDATA, but that's because GRIDDATA has a lot of other machinery to handle sectors & search ellipses. In fact, if you *do* use sectors or search_ellipse, then GRIDDATA has to revert to the old slow algorithm with the ludc in the inner loop. Oh well.

Anyway, let me know how this code looks. If all goes well, this will make it into IDL 8.3, due out in a month or so.

Mike, thanks again for the patch to the code.

Cheers, Chris **ExelisVIS** ; Copyright (c) 1993-2013, Exelis Visual Information Solutions, Inc. All rights reserved. Unauthorized reproduction is prohibited. ;Return Exponential Covariance Fcn $C(d) = C1 \exp(-3 d/A)$ if d!= 0 = C1 + C0 if d == 0FUNCTION Krig_expon, d, t COMPILE_OPT idl2, hidden r = t[2] * exp((-3./t[0]) * d)r[WHERE(d eq 0, /NULL)] = t[1] + t[2]return, r end ;Return Spherical Covariance Fcn $C(d) = C1 [1 - 1.5(d/A) + 0.5(d/A)^3]$ if d < A= C1 + C0 if d == 0= 0if d > A

```
FUNCTION Krig_sphere, d, t
 COMPILE_OPT idl2, hidden
 ; The clipping to < 1 will handle the case d > A, so that v = 0.
 r = d/t[0] < 1
 v = t[2]*(1 - r*(1.5 - 0.5*r*r))
 v[WHERE(r eq 0, /NULL)] = t[1] + t[2]
 return. v
end
  CT, VIS, Oct 2013: Per Mike's suggestion, speed up the algorithm by
    moving LUSOL out of the loops, and vectorizing the inner loop.
    Add DOUBLE, XOUT, YOUT keywords.
    Fix the spherical covariance computation for d > A.
FUNCTION krig2d, z, x, y, $
 DOUBLE=doubleIn, $
 REGULAR = regular, XGRID=xgrid, $
 XVALUES = xvalues, YGRID = ygrid, YVALUES = yvalues, $
 GS = gs, BOUNDS = bounds, NX = nx0, NY = ny0, $
 EXPONENTIAL = exponential, SPHERICAL = spherical, $
 XOUT=xout, YOUT=yout
 compile_opt idl2, hidden
 on error, 2
 s = size(z); Assume 2D
 nx = s[1]
 ny = s[2]
 reg = keyword_set(regular) or (n_params() eq 1)
 dbl = KEYWORD_SET(doubleIn)
 if n_elements(xgrid) eq 2 then begin
  x = (dbl ? dindgen(nx) : findgen(nx)) * xgrid[1] + xgrid[0]
  reg = 1
 endif else if n_elements(xvalues) gt 0 then begin
  if n elements(xvalues) ne nx then $
   message, 'Xvalues must have '+string(nx)+' elements.'
  x = xvalues
  reg = 1
 endif
 if n_elements(ygrid) eq 2 then begin
  y = (dbl ? dindgen(ny) : findgen(ny)) * ygrid[1] + ygrid[0]
```

```
reg = 1
endif else if n elements(yvalues) gt 0 then begin
 if n_elements(yvalues) ne ny then $
  message. 'Yvalues must have '+string(ny)+' elements.'
 y = yvalues
 reg = 1
endif
if reg then begin
 if s[0] ne 2 then message, Z array must be 2D for regular grids'
 if n elements(x) ne nx then x = findgen(nx)
 if n elements(y) ne ny then y = findgen(ny)
 x = x \# replicate(dbl ? 1d : 1., ny); Expand to full arrays.
 y = replicate(dbl ? 1d : 1.,nx) # y
endif
n = n elements(x)
if n ne n_elements(y) or n ne n_elements(z) then $
 message, 'x, y, and z must have same number of elements.'
if keyword_set(exponential) then begin
                                           ;Get model params
 t = exponential
 fname = 'KRIG EXPON'
endif else if keyword_set(spherical) then begin
 t = spherical
 fname = 'KRIG SPHERE'
endif else MESSAGE, 'Either EXPONENTIAL or SPHERICAL model must be selected.'
if n elements(t) eq 2 then begin ;Default value for variance?
 mz = total(z) / n; Mean of z
 var = total((z - mz)^2, DOUBLE=dbl)/n; Variance of Z
 t = [t, var-t[1]]; Default value for C1
endif
m = n + 1
            ;# of eqns to solve
a = dbl ? dblarr(m, m) : fltarr(m, m)
; Construct the symmetric distance matrix.
for i=0, n-2 do begin
 i = [i:n-1]; do the columns all at once
 d = (x[i]-x[i])^2 + (y[i]-y[i])^2; Distance squared
 :symmetric
 a[i,j] = d
 a[j,i] = d
endfor
                                       ;Get coefficient matrix
a = call_function(fname, sqrt(a), t)
                  ;Fill edges
a[n,*] = 1.0
```

```
a[*,n] = 1.0
 a[n,n] = 0.0
 LUDC, a, indx, DOUBLE=dbl
                                     ;Solution using LU decomposition
 if n_{elements}(nx0) le 0 then nx0 = 26; Defaults for nx and ny
 if n elements(nv0) le 0 then nv0 = 26
 xmin = min(x, max = xmax); Make the grid...
 ymin = min(y, max = ymax)
 if n elements(bounds) It 4 then bounds = [xmin, ymin, xmax, ymax]
 if n_elements(gs) It 2 then $ ;Compute grid spacing from bounds
  gs = [(bounds[2]-bounds[0])/(nx0-1.), (bounds[3]-bounds[1])/(ny0-1.)]
 : Subtract off a fudge factor to lessen roundoff errors.
 nx = ceil((bounds[2]-bounds[0])/gs[0] - 1e-5)+1;# of elements
 ny = ceil((bounds[3]-bounds[1])/gs[1] - 1e-5)+1
 xout = bounds[0] + gs[0]*(dbl? DINDGEN(nx) : FINDGEN(nx))
 yout = bounds[1] + qs[1]*(dbl ? DINDGEN(ny) : FINDGEN(ny))
 ; One extra for Lagrange constraint
 d = dbl ? DBLARR(m) : FLTARR(m)
 result = dbl ? DBLARR(nx,ny,/nozero) : FLTARR(nx,ny,/nozero)
 az = LUSOL(a, indx, [REFORM(z,N ELEMENTS(z)),0.0], DOUBLE=dbl)
 az = REBIN(TRANSPOSE(az), nx, n+1)
 xx = (SIZE(x, /N_DIM) eq 2) ? x : REBIN(TRANSPOSE(x), nx, n)
 dxsquare = (xx - REBIN(xout, nx, n))^2
 yy = (SIZE(y, /N_DIM) eq 2) ? y : REBIN(TRANSPOSE(y), nx, n)
 ; Do each row separately
 for j=0,ny-1 do begin
  v0 = vout[i]
  ; Do all of the columns in parallel
  d = sqrt(dxsquare + (yy - y0)^2)
  d = CALL FUNCTION(fname, d, t)
  ; Be sure to add the last row of AZ, which is the Lagrange constraint
  result[*,i] = TOTAL(d*az, 2) + az[*,n]
 endfor
 return, result
end
```

Subject: Re: How to speed up KRIG2D by 30x Posted by David Fanning on Thu, 10 Oct 2013 17:56:49 GMT

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Chris Torrence writes:

> Okay, here is the new code, minus the comments.

Chris, when I try to compile this code in IDL 8.2.3 I get this:

IDL> .compile -v 'krig2d.pro'

% Compiled module: KRIG_EXPON. % Compiled module: KRIG_SPHERE.

j = [i:n-1]; do the columns all at once

% Syntax error.

At: C:\IDL\krig2d.pro, Line 106

Cheers,

David

--

David Fanning, Ph.D.

Fanning Software Consulting, Inc.

Coyote's Guide to IDL Programming: http://www.idlcoyote.com/

Sepore ma de ni thue. ("Perhaps thou speakest truth.")

Subject: Re: How to speed up KRIG2D by 30x

Posted by David Fanning on Thu, 10 Oct 2013 18:27:51 GMT

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Chris Torrence writes:

> Anyway, let me know how this code looks. If all goes well, this will make it into IDL 8.3, due out in a month or so.

Substituting this:

$$i = Lindgen((n-1) - i) + i$$

For this (which doesn't compile):

I find that the new version runs about 80 times faster than the old

versioin. But, I also find that the results are different:

```
IDL> minmax, z1; Old version
MinMax: -0.139365 4.87036
IDL> minmax, z2; New version
MinMax: 0.954356 5.97115
```

Any ideas on how to account for this? Displaying the two arrays as images side-by-side shows the differences.

Cheers,

David

David Fanning, Ph.D.
Fanning Software Consulting, Inc.
Coyote's Guide to IDL Programming: http://www.idlcoyote.com/
Sepore ma de ni thue. ("Perhaps thou speakest truth.")

Subject: Re: How to speed up KRIG2D by 30x Posted by chris_torrence@NOSPAM on Thu, 10 Oct 2013 20:04:24 GMT View Forum Message <> Reply to Message

```
On Thursday, October 10, 2013 12:27:51 PM UTC-6, David Fanning wrote:
> Chris Torrence writes:
>
>
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>
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>
>
>
>
    j = Lindgen((n-1) - i) + i
>
>
>
> For this (which doesn't compile):
>
>
```

```
j=[i:n-1]
>
>
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>
>
>
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> David
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>
  David Fanning, Ph.D.
> Fanning Software Consulting, Inc.
  Coyote's Guide to IDL Programming: http://www.idlcoyote.com/
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  Sepore ma de ni thue. ("Perhaps thou speakest truth.")
Hi David,
Thanks for trying out the code. Whoops! That [i:n-1] is a new IDL 8.3 feature. :-)
```

But I think your replacement code should be: i = LINDGEN(n-i) + i

That probably explains the difference. When I compare the old to the new, I see differences of 10^-5 or less.

-Chris

Subject: Re: How to speed up KRIG2D by 30x Posted by David Fanning on Thu, 10 Oct 2013 20:09:56 GMT View Forum Message <> Reply to Message

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- > But I think your replacement code should be:
- > j = LINDGEN(n-i) + i

>

> That probably explains the difference. When I compare the old to the new, I see differences of 10^-5 or less.

Ah, OK. Works great now. VERY fast! :-)

Thanks,

David

--

David Fanning, Ph.D. Fanning Software Consulting, Inc.

Coyote's Guide to IDL Programming: http://www.idlcoyote.com/

Sepore ma de ni thue. ("Perhaps thou speakest truth.")

Subject: Re: How to speed up KRIG2D by 30x Posted by Mike[5] on Fri, 11 Oct 2013 11:11:45 GMT View Forum Message <> Reply to Message

Hi Chris.

Great job! I confirm that my modified routine using variograms gives identical results to yours within numerical accuracy, as long as I set my variograms=0 when d=0 in agreement with your

covariances. This is of course after translating the interesting new IDL 8.3 feature that David spotted. Note that one can use either variograms functions or covariances without further changes to the program.

The new covariance functions now looks right and corrects for some major numerical differences one can see against the old KRIG2D, when the data extend beyond the region where the covariance was supposed to flatten out.

I like your optimizations in the final loop and the XOUT and YOUT keywords addition. And I am glad you also already modified GRIDDATA. This was an amazing efficient reaction on your side!

Cheers, Michele

> >

>

>

> >

> >

On Thursday, 10 October 2013 18:48:56 UTC+1, Chris Torrence wrote:

> Okay, here is the new code, minus the comments. I added 3 new keywords: DOUBLE, XOUT, YOUT. DOUBLE forces double precision. XOUT, YOUT are output keywords that contain the final X/Y locations. I also vectorized the final loop, for even more speed.

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>
>
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> Mike, thanks again for the patch to the code.
>
>
>
> Cheers,
>
> Chris
> ExelisVIS

Subject: Re: How to speed up KRIG2D by 30x Posted by David Fanning on Sat, 12 Oct 2013 15:28:39 GMT View Forum Message <> Reply to Message

Chris Torrence writes:

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Fast Kriging may have saved the day in a map warping problem I've been working on. This is really, really great! Thanks for being all over this, and thanks to Michele for solving the original problem.

Cheers,

David

--

David Fanning, Ph.D.

Fanning Software Consulting, Inc.

Coyote's Guide to IDL Programming: http://www.idlcoyote.com/

Sepore ma de ni thue. ("Perhaps thou speakest truth.")

Subject: Re: How to speed up KRIG2D by 30x Posted by timothyja123 on Mon, 14 Oct 2013 23:47:51 GMT

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On Sunday, October 13, 2013 2:28:39 AM UTC+11, David Fanning wrote:

> Fast Kriging may have saved the day in a map warping problem I've been

> working on. This is really, really great! Thanks for being all over

> this, and thanks to Michele for solving the original problem.

Thanks to the power of Open Source.

Subject: Re: How to speed up KRIG2D by 30x Posted by David Fanning on Tue, 15 Oct 2013 00:24:39 GMT View Forum Message <> Reply to Message

timothyja123@gmail.com writes:

> Thanks to the power of Open Source.

As opposed to the confusion of Open Source, I presume you mean. But, yes, in this case, it worked out great. ;-)

Cheers,

David

David Fanning, Ph.D. Fanning Software Consulting, Inc.

Coyote's Guide to IDL Programming: http://www.idlcoyote.com/

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