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Subject: Re: Simple MODULO question.  
Posted by [peter](#) on Wed, 03 Jul 1996 07:00:00 GMT  
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S. Penzes (penzes@dres.dnd.ca) wrote:  
: It truly is a simple question and the online help doesn't seem to  
: answer it. So it's either a bug or I have a short circuit in a synapse  
: someplace. Anyway here it is:

: Why does `print,1.0 mod 0.25` return 0.00000 (as expected)  
: generally `1.0 mod (1.0/2^n)` returns 0  
: while `print,1.0 mod 0.2`  
: or `print,1.0 mod (1.0/5.0)` return 0.200000  
: generally `1.0 mod (1.0 / n)`

Probably because, in floating point, 0.25 is represented exactly, so that  $1.0/0.25 = 0.0$ , while 0.2 is not represented exactly. I'll guess that 0.2 is actually something like 0.200000001, so that  $5*0.2$  is greater than 1.0, while  $1.0-4*0.2$  is 0.199999996, which prints at 0.2.

Relying on true equality of floating point numbers as a test (which this is doing, relying on  $5.0*0.2=1.0$ ) is, well, unreliable.

Peter

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Subject: Re: Simple MODULO question.  
Posted by [Peter Mason](#) on Wed, 03 Jul 1996 07:00:00 GMT  
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On 2 Jul 1996, S. Penzes wrote:  
> Why does `print,1.0 mod 0.25` return 0.00000 (as expected)  
> generally `1.0 mod (1.0/2^n)` returns 0  
> while `print,1.0 mod 0.2`  
> or `print,1.0 mod (1.0/5.0)` return 0.200000  
> generally `1.0 mod (1.0 / n)`  
>  
> In case you're wondering, I am trying to determine if:  
> for  $x \bmod y$  whether  $x$  is an integer multiple of  $y$ .

I guess you're experiencing one of the pitfalls of working with floating-point numbers - they're not necessarily exact.  
I'd have to hazard a guess at exactly what's happening in this example:

- . In the first case with  $1.0 \bmod 0.25$ , both 1.0 and 0.25 ( $= 1/8$ ) can be represented exactly in floating-point, and so 0.25 divides an integral number of times into 1.0 and the mod (remainder) is 0.
- . In the second case with  $1.0 \bmod 0.2$ , although 0.2 looks like a simple, exact number in base 10, it is a bit of a headache in base 2 and can't be represented exactly - rather like  $1/3$  in base 10. My guess is that its floating-point representation is fractionally larger than 0.2, and so  $1.0 / "0.2"$  is fractionally less than 5. So  $1.0 \bmod "0.2" = 5.0 - 4 * "0.2"$ , which is fractionally less than 0.2. You can get a hint that there's a problem with: `PRINT,1.0D/0.2`. The result printed is 4.9999999. (This is a fluke of the print formatting, I think - both  $1.0/0.2$  and  $1.0D/0.2D$  return 5!)

I think that you might have to use a steam-driven method for your test:  
Instead of testing  $((x \bmod y) \text{ eq } 0.0)$ , test:  
 $(\text{abs}(x - y * \text{round}(x/y)) \text{ lt } \text{some\_small\_tolerance})$   
or such.

Peter Mason

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